



2011
TRIAL HIGHER SCHOOL CERTIFICATE
EXAMINATION

General Mathematics

General Instructions

- Reading Time- 5 minutes.
- Working Time - 2½ hours.
- Write using a blue or black pen.
- Board approved calculators may be used.
- A Formulae Sheet is provided which may be used throughout the paper.

Section I

Total marks (22)

- Attempt Questions 1-22.
- Answer on the Multiple Choice answer sheet provided.
- Allow about 30 minutes for this section.

Section II

Total marks (78)

- Attempt questions 23 – 28
- Answer in the booklets provided, unless otherwise instructed. Start a new booklet for each question.
- Allow about 2 hours for this section.

Section 1 22 Marks

Attempt all questions

Allow about 30 minutes for this section

Use the multiple choice answer sheet for Questions 1 - 22

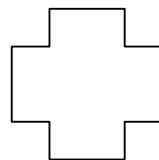
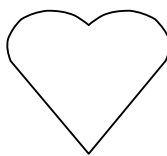
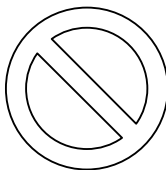
1. The following stem-and-leaf graph represents boys' and girls' heights

Boys		Girls
	15	6 9
9 9	16	0 2 5 8
9 8 7 5	17	1 1 4
7 7 5 3 3 1	18	0
6 4 2	19	
0	20	

What is the range of scores for the girls?

- A. 11
B. 24
C. 31
D. 44
2. A dress is marked down by 20%. If the original price of the dress was \$70.00, how much did it cost after the discount?
- A. \$14
B. \$50
C. \$56
D. \$90
3. $2a \times 2a^2 =$
- A. $4a^2$
B. $4a^3$
C. $16a^2$
D. $16a^6$
4. Which data set satisfies the following three conditions?
- Mode = 8, Median = 4, Range = 12
- A. 4, 4, 8, 12
B. 1, 4, 4, 13
C. -4, 8, 8, 16
D. -4, 0, 8, 8

5.



In how many ways can these 4 shapes be placed in a row?

- A. 4
- B. 10
- C. 16
- D. 24

6. Given the formula $Q = P^2$, when P increases from -2 to 3, how does Q change?

- A. A decrease of 5
- B. An increase of 5
- C. A decrease of 13
- D. An increase of 25

7. A shop has three flavours of ice-cream to choose from: chocolate, vanilla and strawberry.



What is the probability that Jenny, Sarah and Robert would each choose a vanilla ice-cream from this shop?

- A. $\frac{1}{9}$
- B. $\frac{2}{9}$
- C. $\frac{1}{3}$
- D. $\frac{1}{27}$

8. $12 - 8(x - 2) =$

- A. $28 - 8x$
- B. $4x + 8$
- C. $10 - 8x$
- D. $4x + 2$

9. The weights of a sample of four pieces of empty luggage were recorded as:

3.3 kg, 3.8 kg, 4.2 kg and 4.5 kg

What is the standard deviation (in kg) of this sample, correct to 2 decimal places?

- A. 0.37
B. 0.39
C. 0.45
D. 0.52
10. Sarah works on weekdays after school for 2 hours, Monday to Friday and on Saturdays for 6 hours at time-and-a-half.

Day	Mon	Tue	Wed	Thur	Fri	Sat
Hours	2	2	2	2	2	6

If her normal pay rate is \$12.00 per hour, how much does she earn in a normal week?

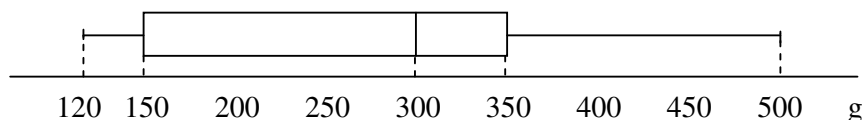
- A. \$126
B. \$168
C. \$192
D. \$228
11. The probability that a new variety of seed will produce flowers in the first year of growth after being planted is 0.4.



200 seeds of this variety are planted.

How many of the seeds are expected to produce flowers in the first year?

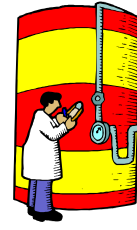
- A. 8
B. 40
C. 80
D. 120
12. 8 000 mail articles were collected from a post office mail box over a weekly period. The box-and-whisker plot shows the weights (in grams) of the article collected.



How many articles collected, weighed between 300 g and 350 g.

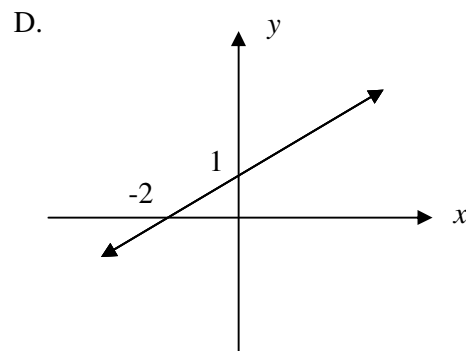
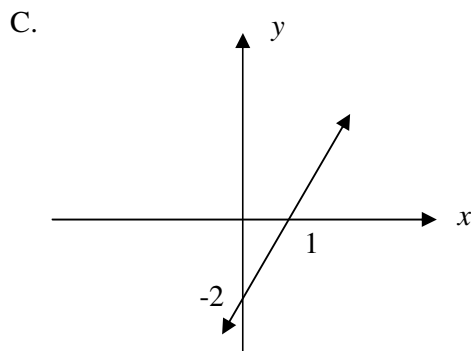
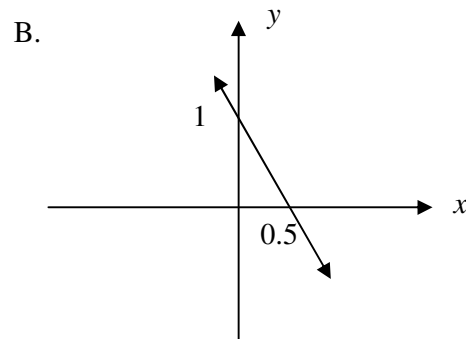
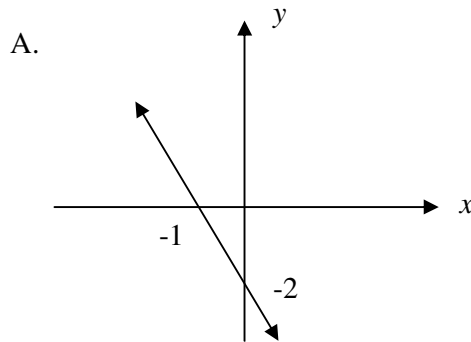
- A. 1 000
B. 2000
C. 2500
D. 4000

13. A tank is being emptied at a rate of 5 litres per minute. At this rate, how long will it take for a kilolitre of water to empty from the tank?



- A. 3 minutes 20 seconds
- B. 20 minutes
- C. 33 minutes 30 seconds
- D. 3 hours 20 seconds

14. Which of the diagrams shows the graph of $y = 1 - 2x$



15. Twelve players try out for a basketball team. There are seven people selected for the team. How many possible teams can be selected?

- A. 7
- B. 12
- C. 84
- D. 792

16. The stopping distance (d) of a car varies directly with the square of the speed (v) of the car. The stopping distance of a car travelling at 90 km/h is 45 metres.

Which of the following represents the correct relationship between d (metres) and v (km/h)?

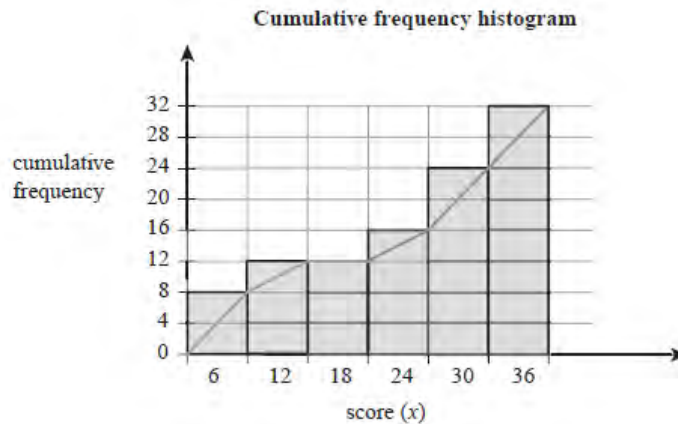
- A. $2d = 45v^2$
- B. $45d = 2v^2$
- C. $d = 180v^2$
- D. $180d = v^2$

17. The income tax rates below were applied in the 2008 - 2009 financial year.

Taxable income	Tax on this income
\$1 - \$6 000	nil
\$6 001 - \$34 000	15c for each \$1 over \$6000
\$34 001 - \$80 000	\$4200 plus 30c for each \$1 over \$34 000
\$80 001 - \$180 000	\$18 000 plus 40c for each \$1 over \$80 000
\$180 001 and over	\$58 000 plus 45c for each \$1 over \$180 000

Helen earned a gross income of \$82 000 and had allowable deductions to the value of \$2500. Calculate the income tax payable for Helen's taxable income.

- A. \$17 850
 B. \$18 600
 C. \$18 800
 D. \$32 800
18. Calculate interquartile range for the data presented in the cumulative histogram below.



- A. 24
 B. 28
 C. 32
 D. 36
19. A sporting event is being played in London and broadcast in Sydney.

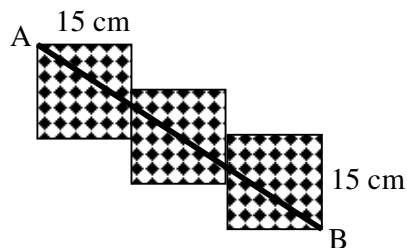
Location	Longitude
London	0°
Sydney	150° E

ABC Sydney broadcasts the start of play at 1:30 am Sunday local time live from London.

What time is it in London at the start of play?

- A. 10:00 pm on Saturday
 B. 3:30 pm on Saturday
 C. 11:30 am Sunday
 D. 11:00 pm on Sunday

20. In a floor design three identical square tiles of side length 15 cm are placed on the floor as shown below.



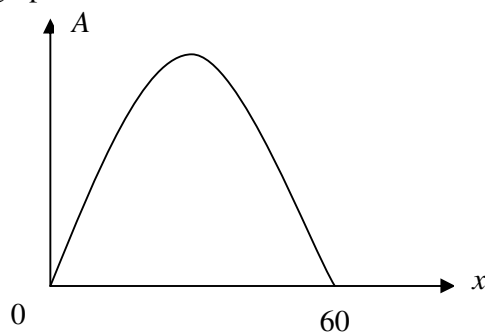
Each tile is placed exactly half way along the side of the tile next to it.
What is the distance in centimetres between the corners A and B of the tiles in the pattern shown?

- A. 21.2
B. 42.4
C. 45
D. 54.1
21. Steve borrows \$5600 to buy a car. The simple interest rate is 10.75% pa and he takes the loan over 3 years. His monthly payment is
- A. \$50.17
B. \$172.28
C. \$205.72
D. \$2468.67
22. A farmer can determine the area (A) in square metres of a rectangular farm by using the formula:

$$A = x(60 - x)$$

where x represents the length of the farm (in metres).

The formula can be graphed as below:



What is the maximum area (in square metres) of the farm?

- A. 60
B. 900
C. 1800
D. 3600

Section 2

Questions 23 – 28 Total Marks (78)

Allow about 2 hours for this section

Answer each question in a new booklet

Question 23 (13 Marks)

Marks

- a. Electricity charges for households are based on the average daily usage of kilowatts per hour (kWh) over a period of 90 days.

A different rate for ‘domestic’ usage and ‘off-peak’ usage is applied:

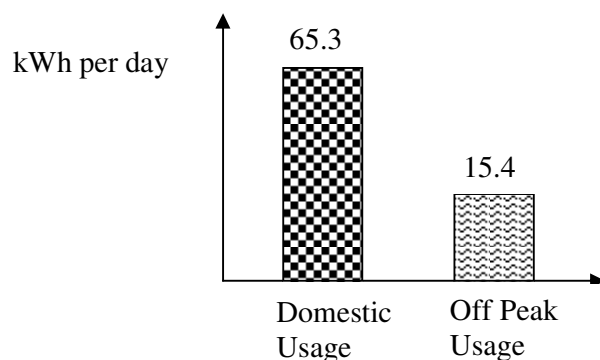
Domestic Usage: \$0.119397 per kWh for the first 1880 kWh

\$0.124267 per kWh for usage over 1880 kWh

Off Peak Usage: \$0.044988 per kWh

A 10% Goods and Services Tax (GST) is added to the total.

The graphs show a household’s average daily usage of electricity for the last 90 days.



- i. Calculate the charge for the ‘domestic’ usage of electricity for this household for the 90 days.
- ii. Calculate the charge for the ‘off peak’ usage
- ii. What is the total charge for electricity usage for this household for the last 90 days?

2

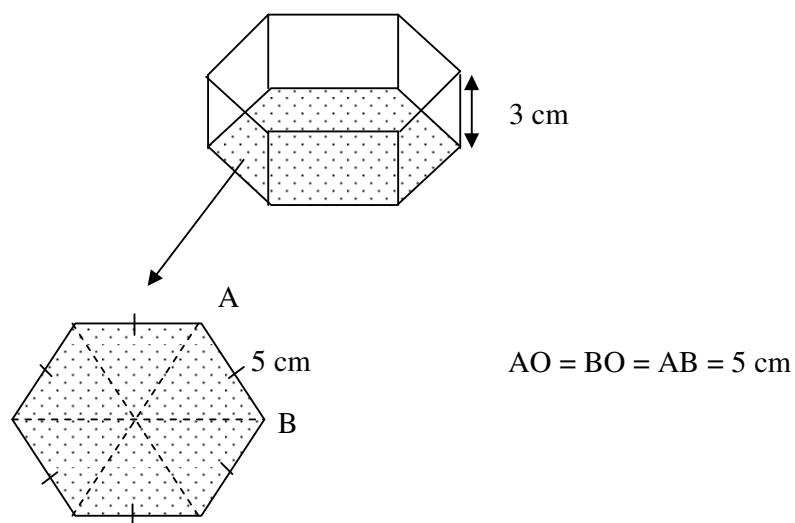
1

2

- (b) A hexagonal prism made completely from thin glass is open at the top.

Marks

The prism has a height of 3 cm and a regular hexagonal base with edges 5 cm (shown below).



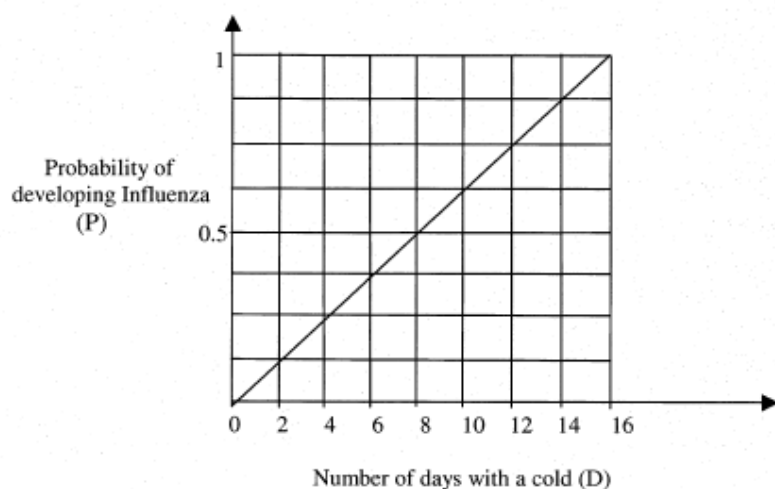
- i. Explain why angle AOB is 60° 1
- ii. Use the formula $\text{Area} = \frac{1}{2}ab \sin c$ to determine the area of triangle ABO to the nearest square centimetre. 2
- iii. Find the area of the hexagonal base of the prism. 1
- iv. Determine the volume of the prism 2
- v. Determine the area (in cm^2) of the glass used in the construction of the prism. 2

Question 24 (13 Marks)**Use a new booklet****Marks**

- a. A company manager earns an annual salary of \$80 100 and is paid each fortnight.
- From each fortnight's gross salary, the manager has deductions of \$440 for superannuation, and \$815 in taxation.
- i. What is the manager's gross fortnightly salary? 1
- ii. Calculate the manager's normal net fortnightly salary. 1
- iii. In the pay for the last fortnight of the year, the manager is paid an additional 17.5% of his gross salary for 2 weeks as his annual holiday loading.
- Determine the gross amount of the holiday loading. 2
- iv. If the holiday loading is taxed at a rate of 27.65%, determine the manager's net salary for the last fortnight of the year. 2

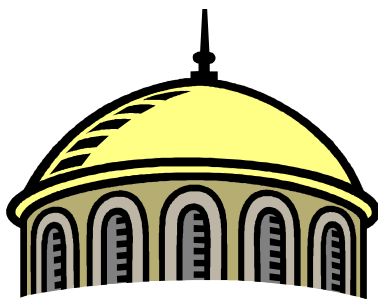
Question 24 continues on the next page

- b. The probability that a person will develop influenza if they have had a cold continuously for a number of days, is shown on the graph below: **Marks**



- i. What probability corresponds to one division on the vertical scale? 1
- ii. After how many days with a cold will a person be certain to develop influenza? 1
- iii. What is the probability that a person will develop influenza after 10 continuous days with a cold? 1
- iv. Amy has had a cold for 2 days and her brother Tim has had a cold for 8 days.
What is the probability that both Amy and Tim will develop influenza? 1
- v. When a doctor administers an annual influenza injection to patients, the probability of developing influenza is halved.
What is the probability that a patient, who has an injection, will develop influenza after 12 days with a cold? 2
- vi. Comment on the likelihood of a patient who has had an injection after 1 day with a cold, developing influenza. 1

- a. A hemispherical dome of diameter 58 metres forms the roof of a building.



- i. Calculate the volume of the roof to the nearest cubic metre. 2
- ii. The density of the hemisphere is given by the formula.

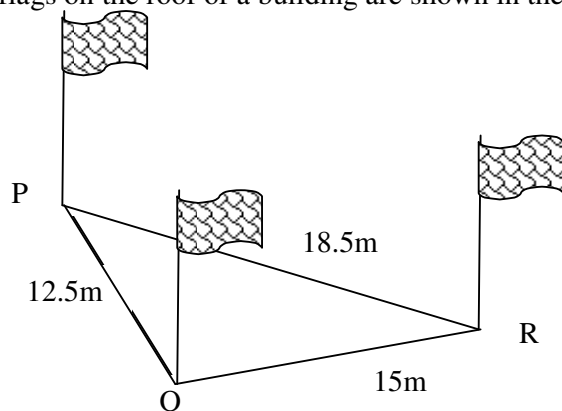
$$\text{density} = \frac{\text{mass}}{\text{volume}} \quad \text{measured in tonnes/m}^3$$

Calculate the mass of the roof if its density is 75.5 kg/m^3 2

- iii. The interior surface of the hemispherical roof is covered with mosaic tiles measuring 6 cm by 6 cm.

By calculating the surface area of the roof, determine approximately the number of tiles used. 2

- b. Three flags on the roof of a building are shown in the diagram below.



- i. Explain why $\angle PQR$ is the largest angle in the triangle formed by the flags. 1
- ii. Calculate the size of this angle to the nearest degree. 3
- iii. Determine the size of $\angle PRQ$ to the nearest degree 2
- iv. If the flag pole at R is due east of the flag pole at Q , determine the bearing of the flag pole at P from R . 1

Question 26 (13 Marks)**Use a new booklet****Marks**

- a. The maximum temperature recorded each month for two towns is shown in the table below:

Month	J	F	M	A	M	J	J	A	S	O	N	D
Town A	31	30	28	26	23	18	17	19	24	27	28	30
Town B	36	34	30	26	22	17	13	20	25	27	32	35

- i. Find for each town the
mean,
mode and
median temperature 3
- ii. Find for each town the
range
interquartile range
standard deviation of the temperature 3
- iii. Using the same scale, draw a box and whisker plot for each town 3
- iv. Write a short description comparing the temperatures in each town 1
- b. The length in metres of a sound wave varies inversely with the number of vibrations of the wave per second.
- A wave of length 20.75 m produces 16 vibrations per second.
- Calculate the number of vibrations per second produced by a wave of length 13.28 m 3

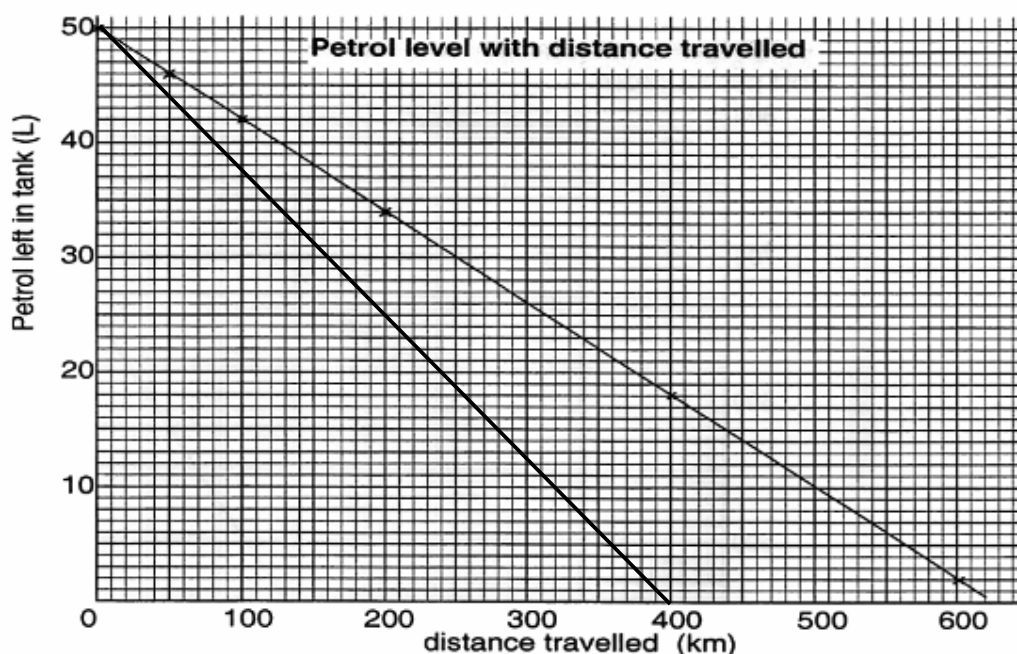
Question 27 (13 Marks)

Use a new booklet

Marks

- a. The graph below shows a comparison of petrol usage for two vehicles with the same fuel tank capacity over distances travelled.

Vehicle A _____ Vehicle B _____

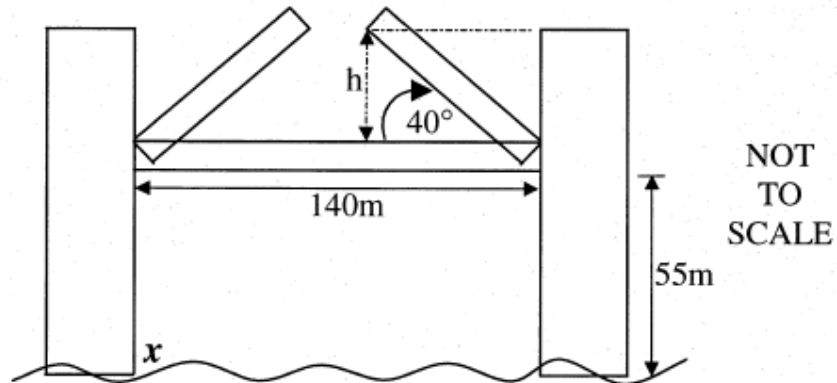


- What is the capacity of the fuel tanks of the two vehicles? 1
- Which vehicle uses less petrol per kilometre? 1
- What distance does vehicle B travel on a full tank of petrol? 1
- What is the fuel consumption in L/100km for vehicle A? 1
- What is the difference in petrol usage between the two vehicles after 200 km? 1
- After 20 litres of petrol have been used in both vehicles, what extra distance has vehicle B travelled? 1
- The petrol (P) remaining in the fuel tank of vehicle A after travelling d km can be represented by the equation $P = 50 - nd$.
What is the value of n in this equation? 1

Question 27 continues on the next page

- b. The 140 metre walkway between the pylons of the bridge opens up to allow ships to pass underneath. **Marks**

The two sections of the walkway are elevated at an angle of 40° and open to a height, h metres above their original horizontal position, so that they are exactly in line with the top of the pylons.



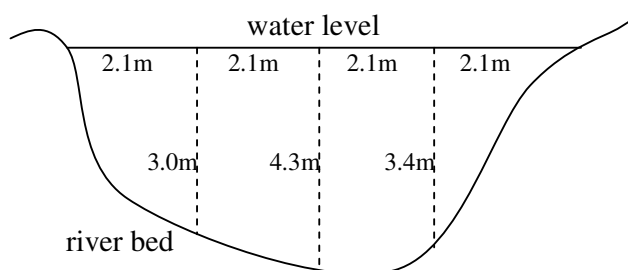
- i. Calculate the height (h) that the sections of the walkway reach above their original horizontal positions. (Give your answer to the nearest metre). **2**
- ii. The walkway is 55 metres above the water line
- Determine the height of the pylon from the water line. **1**
- iii. Determine the angle of elevation of the walkway from the water line at point x . (Give your answer to the nearest degree). **3**

Question 28 (13 Marks)**Use a new booklet****Marks**

- a. A formula relating H and k is given by:

$$H = 6 + 2k^3$$

- i. Find the value of k if $H = 60$ 1
- ii. If k doubles in value, determine the percentage change in H 2
- b. The diagram shows a vertical cross-section of a river.



- i. Use two applications of Simpson's rule to find the approximate area of the river's cross-section. 3
- ii. Estimate the volume of water, in cubic metres, in a 50-metre length of the river, assuming the cross-section is the same as above and uniform along the 50-metre length. Give your answer to the nearest cubic metre. 1
- iii. Estimate the volume of water, in litres, to pass through this cross-section in one hour if the river flows at a rate of 0.35 m/s. Give your answer to the nearest thousand litres. 2
- c. The city of Osaka, Japan (J) has co-ordinates (37°N , 135°E) and Alice Springs in Northern Territory, Australia (A) has co-ordinates (23°S , 135°E).
- i. Determine the size of the angle JOA where O is the centre of the Earth, 1
- ii. Calculate the distance between Osaka and Alice Springs to the nearest kilometre. (Assume the radius of the Earth is 6400km) 2
- iii. A plane travels between the two cities at an average speed of 685km/h. Calculate the flight time in hours and minutes 1

1. B	2. C	3. B	4. D	5. D	6. B	7. D	8. A	9. D	10. D	11. C
12. B	13. D	14. B	15. D	16. D	17. A	18. A	19. B	20. D	21. C	22. B

= 5877 kWh

②

①

= \$78.35

②

①

$$= 10.825 \dots$$

②

①

②

②

①

①

②

②

- b. (i) One vertical unit = 0.125 ①
- (ii) certain flu after 16 days ①
- (iii) $P(\text{flu after 10 days}) = 0.625$ ①
- (iv) $P(\text{Amy and Tim have flu}) = 0.125 \times 0.5$
 $= 0.0625$ ①
- (v) $P(\text{flu after 12 days and injection}) = 0.5 \times 0.75$
 $= 0.375$ ②
- (v) Since the probability of getting flu after one day is half of one unit ie 0.0625, after having an injection this chance would be halved, ie 0.03125. This would make the chance of getting the flu very unlikely. ①

25. a. (i) Volume of dome $= 0.5 \times \frac{3}{4} \times \pi \times 29^3$
 $= 51\,080.2\dots$
 $= 51\,080 \text{ m}^3$ ②

(ii) $75.5 \text{ kg} = 0.075 \text{ T}$
 $0.0755 = \frac{M}{51080}$
 $M = 0.0755 \times 51080$
 $= 3856.54 \text{ tonnes}$ ②

(iii) Surface area $= 0.5 \times 4 \times \pi \times 29^2$
 $= 5284.1588\dots$
 $= 5284 \text{ m}^2 \text{ (to nearest metre)}$
Area tile $= 0.06 \times 0.06$
 $= 0.0036 \text{ m}^2$
Number of tiles needed $= 5284.1588 \div 0.0036$
 $= 1467821.9\dots$
 $= 1\,468\,000 \text{ to nearest thousand}$ ②

- b. (i) The largest angle is opposite the longest side. Since 18.5 cm is the longest side, $\angle PQR$ is the largest angle ①

(ii) $\cos Q = \frac{12.5^2 + 15^2 - 18.5^2}{2 \times 12.5 \times 15}$
 $= 0.104$
 $Q = 84.03\dots$
 $Q = 84^\circ \text{ to nearest degree}$ ③

(iii) $\frac{\sin R}{12.5} = \frac{\sin 84^\circ}{18.5}$
 $\sin R = 0.67197\dots$
 $R = 42.2196\dots$
 $R = 42^\circ \text{ to nearest degree}$ ②

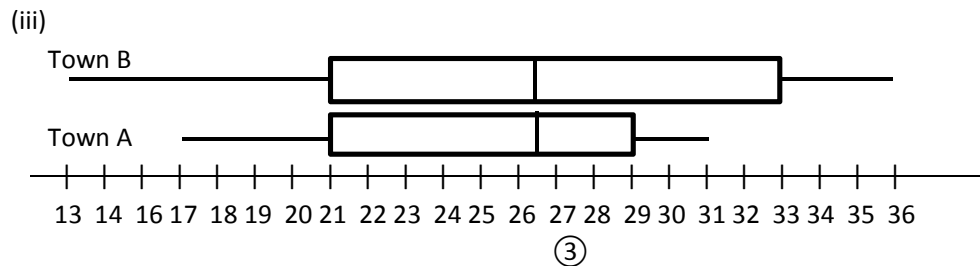
(iv) Bearing of P from R = $270^\circ + 42^\circ$
 $= 312^\circ$ ①

26. a. (i) Town A mean = 25.08
mode = 28, 30
median = 26.5

Town B mean = 26.42
mode = none
median = 26.5 ③

(ii) Town A range = $31 - 17$
 $= 14$
interquartile range = $29 - 21$
 $= 8$
standard deviation = 4.68

Town B range = $36 - 13$
 $= 23$
interquartile range = $33 - 21$
 $= 12$
standard deviation = 7.06 ③



(iv) While the median temperature for Town A and Town B is the same, there is a greater range and interquartile range for Town B compared to Town A. This can also be seen in the differences in standard deviation. ①

b. $l = \frac{k}{v}$ $20.75 = \frac{k}{16}$
 $k = 20.75 \times 16$
 $= 332$
 $l = \frac{332}{v}$ $13.28 = \frac{332}{v}$
 $v = \frac{332}{13.28}$
 $= 25 \text{ vibrations/s}$ ③

27. a. (i) 50L (ii) Vehicle B (iii) 620km (iv) 12 L/100 km (v) 9L
(vi) 90 km (vii) $P = 50 - nd$ $P = 0, d = 400$
 $0 = 50 - n \times 400$
 $n = \frac{50}{400}$
 $= 0.125$ ① each part

b. (i) $\sin 40^\circ = \frac{h}{70}$
 $h = 70 \times \sin 40^\circ$
 $= 45 \text{ m}$ ②

(ii) Pylon height = $45 + 55$
 $= 100 \text{ m}$ ①

(iii) $\tan \theta = \frac{55}{140}$
 $\theta = 21^\circ$
angle of elevation is 21° ③

28. a. (i) $H = 6 + 2k^3$
 $60 = 6 + 2k^3$
 $56 = 2k^3$
 $27 = k^3$
 $k = 3$ ①

(ii) if $k = 6$, $H = 6 + 2 \times 6^3$
 $= 438$
Increase in $H = 438 - 60$
 $= 378$
changed = $\frac{378}{60} \times 100 \%$
 $= 630\%$ ②

b. (i) $A = \frac{2.1}{3} [0 + 4 \times 3 + 4.3] + \frac{2.1}{3} [4.3 + 4 \times 3.4 + 0]$
 $= 23.94 \text{ m}^2$ ③

(ii) $V = 50 \times 23.94$
 $= 1197 \text{ m}^3$ ①

(iii) $0.35 \text{ m/s for 1 hour}$
 $0.35 \times 60 \times 60 = 1260 \text{ m}$
 $V = 1260 \times 23.94$
 $= 30164 \text{ m}^3$
 $= 30164000 \text{ L}$ ②

c. (i) $\angle JOA = 37 + 23$
 $= 60^\circ$ ①

(ii) distance = $\frac{60}{360} \times 2 \times \pi \times 6400$
 $= 6702 \text{ km}$ ②

(iii) $\frac{6702}{685} = 9.78 \text{ hrs}$
 $= 9 \text{ hours } 47 \text{ minutes}$ ①